

# Package ‘bcp’

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**Description** Provides an implementation of the Barry and Hartigan (1993) product partition model for the normal errors change point problem using Markov Chain Monte Carlo. It also extends the methodology to regression models on a connected graph (Wang and Emerson, 2015); this allows estimation of change point models with multivariate responses. Parallel MCMC, previously available in bcp v.3.0.0, is currently not implemented.

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bcp-package	<i>Bayesian Analysis of Change Point Problems</i>
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### Description

Provides an implementation of the Barry and Hartigan (1993) product partition model for the normal errors change point problem using Markov Chain Monte Carlo. It also (i) extends the methodology to regression models on a connected graph (Wang and Emerson, 2015) and (ii) allows estimation of change point models with multivariate responses. Parallel MCMC, previously available in bcp v.3.0.0, is currently not implemented.

### Author(s)

Xiaofei Wang, Chandra Erdman, and John W. Emerson

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bcp	<i>Performs a Bayesian analysis of change point problems</i>
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### Description

bcp() implements the Bayesian change point analysis methods given in Wang and Emerson (2015), of which the Barry and Hartigan (1993) product partition model for the normal errors change point problem is a specific case. 1. Multivariate (or univariate) Bayesian change point analysis: We assume there exists an unknown partition of a data series  $y$  into blocks such that the mean is constant within each block. In the multivariate case, a common change point structure is assumed; means are constant within each block of each sequence, but may differ across sequences within a given block. Conditional on the partition, the model assumes that observations are independent, identically distributed normal, with constant means within blocks and constant variance throughout each sequence. 2. Linear regression Bayesian change point analysis: As with the previous model, we assume the observations  $(x,y)$ , where  $x$  may be multivariate, are partitioned into blocks, and that linear models are appropriate within each block.

If an adjacency structure is provided, the data are assumed to reside on nodes of a graph with the given adjacency structure; additional parameters are used in this graph change point model. If no adjacency structure is provided, the data are assumed to be sequential and the blocks are forced to be contiguous.

**Usage**

```
bcp(y, x = NULL, id = NULL, adj = NULL, w0 = NULL, p0 = 0.2,
    d = 10, burnin = 50, mcmc = 500, return.mcmc = FALSE,
    boundaryType = "node", p1 = 1, freqAPP = 20, nreg = -1)
```

**Arguments**

y	a vector or matrix of numerical data (with no missing values). For the multivariate change point problems, each column corresponds to a series.
x	(optional) a matrix of numerical data (with no missing values) representing the predicting variables for a linear regression.
id	(optional) a vector of integers specifying the location ID for each observation in y, starting from location 1.
adj	(optional) an adjacency list. Indexing the observations from 1 to $n$ , the $i$ -th element of the list is a vector of indices (offset by 1) for nodes that share an edge with node $i$ .
w0	(optional) a single numeric value in the multivariate case or a vector of values in the regression case; in both, the value(s), between 0 and 1, is/are the parameter(s) in the uniform prior(s) on the signal-to-noise ratio(s). If no value is specified, the default value of 0.2 is used, as recommended by Barry and Hartigan (1993).
p0	(optional) a value between 0 and 1. For sequential data, it is the parameter of the prior on change point probabilities, $U(0, p0)$ , on the probability of a change point at each location in the sequence; for data on a graph, it is the parameter in the partition prior, $p0^{l(\rho)}$ , where $l(\rho)$ is the boundary length of the partition.
d	(optional) a positive number only used for linear regression change point models. Lower d means higher chance of fitting the full linear model (instead of the intercept-only model); see prior for $\tau_S$ in Wang and Emerson (2015).
burnin	the number of burnin iterations.
mcmc	the number of iterations after burnin.
return.mcmc	logical. If set to TRUE, the posterior means and the partitions in each iteration are returned.
boundaryType	(optional) only applicable for graph change point analysis. Values can be "node" (default) if we count nodes in the boundary length calculation, or "edge" if we count edges in the boundary length calculation. See Wang and Emerson (2015) for details.
p1	(optional) only applicable for graph change point analysis. The proportion of Active Pixel Passes run that are the actual Active Pixel Passes specified in Barry and Hartigan (1994). $p1 = 0$ corresponds to exclusively using the pseudo-Active Pixel Passes given in Wang and Emerson (2015).
freqAPP	(optional) only applicable for graph change point analysis. A positive integer for the number of Active Pixel Passes run in each step of the MCMC algorithm.
nreg	(optional) only applicable for regression; related to parameter d describing the minimum number of observations needed in a block to allow for fitting a regression model. Defaults to $2 \times$ number of predictors.

## Details

The primary result is an estimate of the posterior mean (or its distribution if `return.mcmc` is TRUE) at every location. Unlike a frequentist or algorithmic approach to the problem, these estimates will not be constant within regions, and no single partition is identified as best. Estimates of the probability of a change point at any given location are provided, however.

The user may set `.Random.seed` to control the MCMC iterations.

The functions `summary.bcp`, `print.bcp`, and `plot.bcp` are used to obtain summaries of the results; `legacyplot` is included from package versions prior to 3.0.0 and will only work for univariate change point analyses.

## Value

Returns a list containing the following components:

**data** a copy of the data.

**return.mcmc** TRUE or FALSE as specified by the user; see the arguments, above.

**mcmc.means** if `return.mcmc=TRUE`, `mcmc.means` contains the means for each iteration conditional on the state of the partition.

**mcmc.rhos** if `return.mcmc=TRUE`, `mcmc.rhos` contains the partitions after each iteration. A value of 1 indicates the end of a block.

**blocks** a vector of the number of blocks after each iteration.

**posterior.mean** a vector or matrix of the estimated posterior means. In the regression case, the matrix includes posterior means for the response variable.

**posterior.var** a vector or matrix of the estimated posterior variances. In the regression case, the estimated posterior variances of the response are provided.

**posterior.prob** a vector of the estimated posterior probabilities of changes at each location.

**burnin** the number of burnin iterations.

**mcmc** the number of iterations after burnin.

**w0** see the arguments, above.

**p0** see the arguments, above.

## Author(s)

Xiaofei Wang, Chandra Erdman, and John W. Emerson

## References

1. J. Bai and P. Perron (2003), Computation and Analysis of Multiple Structural Change Models, *Journal of Applied Econometrics*, **18**, 1-22. <http://qed.econ.queensu.ca/jae/2003-v18.1/bai-perron/>.
2. Daniel Barry and J. A. Hartigan (1993), A Bayesian Analysis for Change Point Problems, *Journal of The American Statistical Association*, **88**, 309-19.
3. Daniel Barry and J. A. Hartigan (1994), A Product Partition Model for Image Restoration, *New Directions in Statistical Data Analysis and Robustness*, (Monte Verita : Proceedings of the Cento Stefano Franscini Ascona), Birkhauser, 9-23.

4. Chandra Erdman and John W. Emerson (2008), A Fast Bayesian Change Point Analysis for the Segmentation of Microarray Data, *Bioinformatics*, 24(19), 2143-2148. <https://www.ncbi.nlm.nih.gov/pubmed/18667443>.
5. Chandra Erdman and John W. Emerson (2007), bcp: An R Package for Performing a Bayesian Analysis of Change Point Problems. *Journal of Statistical Software*, 23(3), 1-13. <http://www.jstatsoft.org/v23/i03/>.
6. A. B. Olshen, E. S. Venkatraman, R. Lucito, M. Wigler (2004), Circular binary segmentation for the analysis of array-based DNA copy number data, *Biostatistics*, 5, 557-572. <http://www.bioconductor.org/packages/release/bioc/html/DNAcopy.html>.
7. Snijders *et al.* (2001), Assembly of microarrays for genome-wide measurement of DNA copy number, *Nature Genetics*, 29, 263-264.
8. Xiaofei Wang and John W. Emerson (2015). Bayesian Change Point Analysis of Linear Models on General Graphs, *Working Paper*.
9. Achim Zeileis, Friedrich Leisch, Kurt Hornik, Christian Kleiber (2002), strucchange: An R Package for Testing for Structural Change in Linear Regression Models, *Journal of Statistical Software*, 7(2), 1-38. <http://www.jstatsoft.org/v07/i02/>.

### See Also

[plot.bcp](#), [summary.bcp](#), and [print.bcp](#) for summaries of the results.

### Examples

```
##### univariate sequential data #####
# an easy problem with 2 true change points
set.seed(5)
x <- c(rnorm(50), rnorm(50, 5, 1), rnorm(50))
bcp.1a <- bcp(x)
plot(bcp.1a, main="Univariate Change Point Example")
legacyplot(bcp.1a)

# a hard problem with 1 true change point
set.seed(5)
x <- rep(c(0,1), each=50)
y <- x + rnorm(50, sd=1)
bcp.1b <- bcp(y)
plot(bcp.1b, main="Univariate Change Point Example")

##### multivariate sequential data #####
# an easy problem in k=3 dimensions
set.seed(5)
x <- rnorm(6, sd=3)
y <- rbind(cbind(rnorm(50, x[1]), rnorm(50, x[2]), rnorm(50, x[3])),
           cbind(rnorm(50, x[4]), rnorm(50, x[5]), rnorm(50, x[6])))
bcp.2a <- bcp(y)
plot(bcp.2a, main="Multivariate (k=3) Change Point Example")
plot(bcp.2a, separated=TRUE, main="Multivariate (k=3) Change Point Example")

# a harder problem in k=5 dimensions
```

```

set.seed(5)
means1 <- rep(0, 5)
means2 <- rep(1, 5)
x <- rbind(matrix(rep(means1, each=50), nrow=50),
            matrix(rep(means2, each=50), nrow=50))
y <- x + rnorm(length(x), sd=1)
bcp.2b <- bcp(cbind(y))
plot(bcp.2b, main="Multivariate (k=5) Change Point Example")

##### linear models with sequential data #####
# 1 true change point at location 50; the predicting variable x is not related to location
x <- rnorm(100)
b <- rep(c(3,-3), each=50)
y <- b*x + rnorm(100)
bcp.3a <- bcp(y, x)
# in the two plots that follow, the location IDs are used as the plot characters
par(mfrow=c(1,2))
plot(y ~ x, type="n", main="Linear Regression: Raw Data")
text(x, y, as.character(1:100), col=(b/3)+2)
plot(y ~ x, type="n", main="Linear Regression: Posterior Means")
text(x, bcp.3a$posterior.mean[,1], as.character(1:100), col=(b/3)+2)
plot(bcp.3a, main="Linear Regression Change Point Example")

# 1 true change point at location 50; the predicting variable x is equal to location
x <- 1:100
b <- rep(c(3,-3), each=50)
y <- b*x + rnorm(100, sd=50)
bcp.3b <- bcp(y, x)
plot(bcp.3b, main="Linear Regression Change Point Example")

##### univariate data on a grid #####
## Not run:
set.seed(5)
adj <- makeAdjGrid(20)
z <- rep(c(0, 2), each=200)
y <- z + rnorm(400, sd=1)
out <- bcp(y, adj=adj, burnin=500, mcmc=500)

if (require("ggplot2")) {
  df <- data.frame(mean=z, data = y, post.means = out$posterior.mean[,1],
                  post.probs = out$posterior.prob,
                  i = rep(1:20, each=20), j = rep(1:20, times=20))

  # visualize the means
  g <- ggplot(df, aes(i,j)) +
    geom_tile(aes(fill = mean), color='white') +
    scale_fill_gradientn(limits=range(y), colours=c('white', 'steelblue'))+
    ggtitle("True Means")
  print(g)

  # visualize the data
  g <- ggplot(df, aes(i,j)) +
    geom_tile(aes(fill = data), color='white') +

```

```

        scale_fill_gradientn(limits=range(y), colours=c('white', 'steelblue'))+
        ggtitle("Observed Data")
print(g)

# visualize the posterior means/probs
g <- ggplot(df, aes(i,j)) +
  geom_tile(aes(fill = post.means), color='white') +
  scale_fill_gradientn(limits=range(y), colours=c('white', 'steelblue'))+
  ggtitle("Posterior Means")
print(g)

g <- ggplot(df, aes(i,j)) +
  geom_tile(aes(fill = post.probs), color='white') +
  scale_fill_gradientn(limits=c(0, 1), colours=c('white', 'steelblue'))+
  ggtitle("Posterior Boundary Probabilities")
print(g)
}

## End(Not run)

## Not run:
##### multivariate data on a grid #####
set.seed(5)
x <- rnorm(6, sd=3)
y <- rbind(cbind(rnorm(50, x[1]), rnorm(50, x[2]), rnorm(50, x[3])),
           cbind(rnorm(50, x[4]), rnorm(50, x[5]), rnorm(50, x[6])))
adj <- makeAdjGrid(10)
a <- bcp(y, adj=adj, p0=0.4, burnin=500, mcmc=500)

##### linear models on a grid #####
set.seed(5)
x <- rnorm(100)
b <- rep(c(3,-3), each=50)
y <- b*x + rnorm(100)
adj <- makeAdjGrid(10)
a <- bcp(y,x,adj=adj, p0=0.4, burnin=500, mcmc=500)

##### linear models on a grid using pseudo-APPs #####
x <- rnorm(100)
b <- rep(c(3,-3), each=50)
y <- b*x + rnorm(100)
adj <- makeAdjGrid(10)
a <- bcp(y,x,adj=adj, p0=0.4, burnin=500, mcmc=500, p1 = 0)
## End(Not run)

##### univariate data on a graph #####
## Not run:
  demo(bcpgraph)

## End(Not run)

##### Real Data Examples #####
## Not run:

```

```
# Coriell chromosome 11: univariate sequential data
demo(coriell)

# U.S. ex-post interest rate: univariate sequential data
demo(RealInt)

# Lombard: univariate sequential data (with and without linear models)
demo(Lombard)

# Quebec rivers: multivariate sequential data
demo(QuebecRivers)

# New Haven housing: linear models on a graph
demo(NewHaven)

## End(Not run)
```

---

coriell	<i>Array CGH data set of Coriell cell lines</i>
---------	---

---

### Description

These are two data array CGH studies of Coriell cell lines taken from the reference below.

### Usage

```
coriell
```

### Format

A data frame containing five variables: first is clone name, second is clone chromosome, third is clone position, fourth and fifth are log2ratio for two cell lines.

### Source

<http://www.nature.com/ng/journal/v29/n3/full/ng754.html>

### References

1. Olshen, A. B., Venkatraman, E. S., Lucito, R., Wigler, M. (2004), Circular binary segmentation for the analysis of array-based DNA copy number data, *Biostatistics*, **5**, 557-572. url: <http://www.bioconductor.org/packages/release/bioc/html/DNAcopy.html>.
2. Snijders *et al.* (2001), Assembly of microarrays for genome-wide measurement of DNA copy number, *Nature Genetics*, **29**, 263-264.

### Examples

```
demo(coriell)
```



---

fitted.bcp	<i>Extract model fitted values</i>
------------	------------------------------------

---

## Description

fitted method for class bcp.

## Usage

```
## S3 method for class 'bcp'  
fitted(object, ...)
```

## Arguments

object            the result of a call to bcp().  
...                (optional) additional arguments, ignored.

## Value

Fitted values extracted from the bcp object.

## Author(s)

Xiaofei Wang, Chandra Erdman and John W. Emerson

## See Also

[plot.bcp](#), [summary.bcp](#), and [print.bcp](#) for summaries of the results.

## Examples

```
##### A random sample from a few normal distributions #####  
testdata <- c(rnorm(50), rnorm(50, 5, 1), rnorm(50))  
bcp.0 <- bcp(testdata)  
residuals(bcp.0)
```

---

`interval.prob`*Estimate the probability of a change point in a specified interval*

---

### Description

The function `interval.prob()` estimates the probability of at least one change point in the specified interval of sequential observations; it may only be used when `return.mcmc=TRUE`.

### Usage

```
interval.prob(object, start, end)
```

### Arguments

<code>object</code>	the result of a call to <code>bcp()</code> .
<code>start</code>	the starting index of the interval.
<code>end</code>	the ending index of the interval.

### Details

For sequential data only, the function returns an estimate of the posterior probability of at least one change point in the specified interval.

### Note

`return.mcmc` must be `TRUE`.

### Author(s)

Xiaofei Wang, Chandra Erdman, and John W. Emerson

### See Also

[bcp](#) and [plot.bcp](#).

### Examples

```
##### A random sample from a few normal distributions #####
testdata <- c(rnorm(50), rnorm(50, 5, 1), rnorm(50))
bcp.0 <- bcp(testdata, return.mcmc=TRUE)
plot(bcp.0, main="Univariate Change Point Example")
interval.prob(bcp.0, 45, 55)
```

---

`legacyplot`*Plotting univariate Bayesian change point results*

---

## Description

`legacyplot()` produces summary plots of the results of `bcp()` when used for univariate analysis; it was the default method prior to package version 3.0.0.

## Usage

```
legacyplot(x, ...)
```

## Arguments

`x`                    the result of a call to `bcp()`.  
`...`                 (optional) additional arguments, ignored.

## Details

`legacyplot()` produces the following plots using base graphics:

Posterior Means: location in the sequence versus the posterior mean over the iterations.

Posterior Probability of a Change: location in the sequence versus the relative frequency of iterations which resulted in a change point.

## Author(s)

Chandra Erdman and John W. Emerson

## See Also

[plot.bcp](#), [bcp](#), [summary.bcp](#), and [print.bcp](#) for complete results and summary statistics.

## Examples

```
##### A random sample from a few normal distributions #####  
testdata <- c(rnorm(50), rnorm(50, 5, 1), rnorm(50))  
bcp.0 <- bcp(testdata, return.mcmc=TRUE)  
legacyplot(bcp.0)
```

---

lombard

*Milling machine indentation data*

---

### Description

Radii of 100 circular indentations cut by a milling machine.

### Usage

lombard

### Format

A vector of length 100 containing the individual radii.

### Source

The data is available online in the data archive of the *Journal of Applied Econometrics*. url: <http://qed.econ.queensu.ca/jae/2003-v18.1/bai-perron/>.

### References

1. Daniel Barry and J. A. Hartigan (1993), A Bayesian Analysis for Change Point Problems, *Journal of The American Statistical Association*, **88**, 309-19.
2. F. Lombard (1987), Rank Tests for Changepoint Problems, *Biometrika*, **74**, 615-624.

### Examples

```
## Not run:
data(lombard)
# univariate change point analysis
bcp.model <- bcp(lombard, burnin=500, mcmc=5000, return.mcmc=TRUE)

# linear model change point analysis
bcpr.model <- bcp(lombard, cbind(1:100), burnin=500, mcmc=5000, return.mcmc=TRUE)

plot(bcp.model, main="Lombard Milling Data")
plot(bcpr.model, main="Lombard Milling Data (with Regression Model)")

## End(Not run)
```

---

`makeAdjGrid`*Creating the adjacency structure for grid graphs*

---

### Description

`makeAdjGrid()` produces a sparse representation of the adjacency structure for grid graphs, useful as the `adj` argument in `bcp()`.

### Usage

```
makeAdjGrid(n, m = NULL, k = 8)
```

### Arguments

<code>n</code>	the number of rows of vertices in the graph data.
<code>m</code>	(optional) the number of column of vertices in the graph data. If not given, we assume $m = n$ .
<code>k</code>	(optional) the number of neighbors assumed for a typical vertex (see details below), either 4 or 8. Default number of neighbors is assumed to be 8.

### Details

`makeAdjGrid()` produces a list representation of the adjacency structure for grid graphs. The  $i$ -th entry in the list gives a vector of neighbor ids for the  $i$ -th node. Note that neighbor ids are offset by 1 because indexing starts at 0 in C++. If  $k = 8$ , then we assume each node is joined via edges to its 8 neighbors in the (top left, top middle, top right, left, right, bottom left, bottom middle, and bottom right) directions, where applicable. If  $k = 4$ , then we assume each node is joined via edges to its 4 neighbors in the (top, right, bottom, left) directions, where applicable.

### Author(s)

Xiaofei Wang

### See Also

[bcp](#) for performing Bayesian change point analysis.

### Examples

```
# generates an adjacency list for a 10 node by 5 node grid, assuming a maximum of 8 neighbors
adj <- makeAdjGrid(10, 5)
```

```
# generates an adjacency list for a 10 node by 5 node grid, assuming a maximum of 4 neighbors
adj4 <- makeAdjGrid(10, 5, 4)
```

```
### show a grid example
## Not run:
```

```

set.seed(5)
adj <- makeAdjGrid(20)
z <- rep(c(0, 2), each=200)
y <- z + rnorm(400, sd=1)
out <- bcp(y, adj=adj, burnin=500, mcmc=500)

if (require("ggplot2")) {
  df <- data.frame(mean=z, data = y, post.means = out$posterior.mean[,1],
                  post.probs = out$posterior.prob,
                  i = rep(1:20, each=20), j = rep(1:20, times=20))

  # visualize the data
  g <- ggplot(df, aes(i,j)) +
    geom_tile(aes(fill = data), color='white') +
    scale_fill_gradientn(limits=range(y), colours=c('white', 'steelblue'))+
    ggtitle("Observed Data")
  print(g)

  # visualize the means
  g <- ggplot(df, aes(i,j)) +
    geom_tile(aes(fill = mean), color='white') +
    scale_fill_gradientn(limits=range(y), colours=c('white', 'steelblue'))+
    ggtitle("True Means")
  print(g)

  # visualize the posterior means/probs
  g <- ggplot(df, aes(i,j)) +
    geom_tile(aes(fill = post.means), color='white') +
    scale_fill_gradientn(limits=range(y), colours=c('white', 'steelblue'))+
    ggtitle("Posterior Means")
  print(g)

  g <- ggplot(df, aes(i,j)) +
    geom_tile(aes(fill = post.probs), color='white') +
    scale_fill_gradientn(limits=c(0, 1), colours=c('white', 'steelblue'))+
    ggtitle("Posterior Boundary Probabilities")
  print(g)
}

## End(Not run)

```

---

NewHavenHousing

*New Haven housing data*


---

### Description

Location, 2011 assessed value, and physical characteristics for 244 houses in a region of New Haven, CT.

**Usage**

NewHavenHousing

**Format**

A matrix containing location, 2011 assessed value, and physical characteristics in the columns.

**Source**

The data can be scraped from the New Haven, CT Online Assessment Database <http://gis.vgsi.com/newhavenct/>

**References**

Xiaofei Wang and John W. Emerson (2015). Bayesian Change Point Analysis of Linear Models on General Graphs, *Working Paper*.

**Examples**

```
## Not run:  
demo("NewHaven")  
  
## End(Not run)
```

---

plot.bcp

*Plotting Bayesian change point results*

---

**Description**

plot.bcp() produces summary plots of the results of bcp(). Currently, only the summary plots for serial data are implemented. If an adjacency structure (adj) is provided, then the data are assumed to reside on nodes of a general graph. Additional parameters are used in this graph change point model.

**Usage**

```
## S3 method for class 'bcp'  
plot(x, separated = FALSE, outer.margins = list(left =  
  unit(4, "lines"), bottom = unit(3, "lines"), right = unit(2, "lines"),  
  top = unit(2, "lines")), lower.area = unit(0.33, "npc"),  
  size.points = unit(0.25, "char"), pch.points = 20, colors = NULL,  
  main = NULL, xlab = NULL, yaxlab = NULL,  
  cex.axes = list(cex.xaxis = 0.75, cex.yaxis.lower = 0.75,  
  cex.yaxis.upper.default = 0.75, cex.yaxis.upper.separated = 0.5),  
  lwd = 1, ...)
```

**Arguments**

<code>x</code>	the result of a call to <code>bcp()</code> .
<code>separated</code>	logical. If set to <code>TRUE</code> and the data is multivariate, each series is plotted separately.
<code>outer.margins</code>	(optional) list of units specifying the left, bottom, right and top margins. For more information on units, see the documentation for <code>grid</code> .
<code>lower.area</code>	(optional) unit specifying the proportion of the plot occupied by the posterior probabilities of change points.
<code>size.points</code>	(optional) unit specifying the size of the data points.
<code>pch.points</code>	(optional) unit specifying the style of the data points.
<code>colors</code>	(optional) vector specifying the colors in which to plot each data series.
<code>main</code>	(optional) plot title. Use <code>""</code> for no title.
<code>xlab</code>	(optional) a character string specifying the x-axis label. Defaults to "Location".
<code>xaxlab</code>	(optional) a vector having length equal to the number of observations giving the x-axis tick labels. Defaults to the sequence from 1 to n.
<code>cex.axes</code>	(optional) list specifying the sizes of the axes labels. <code>cex.xaxis</code> specifies the size of the x-axis label, <code>cex.yaxis.lower</code> specifies the size of the y-axis label of the posterior probability plot, <code>cex.yaxis.upper.default</code> specifies the size of the y-axis labels of the posterior means plot when the series are displayed in a single plot, and <code>cex.yaxis.upper.separated</code> specifies the size of the y-axis labels of the posterior means plots when each series is plotted separately.
<code>lwd</code>	line width
<code>...</code>	(optional) additional arguments, ignored.

**Details**

`plot.bcp()` produces the following plots using `grid` graphics instead of `base`:

Posterior Means: location in the sequence versus the posterior means over the iterations.

Posterior Probability of a Change: location in the sequence versus the relative frequency of iterations which resulted in a change point.

**Author(s)**

Xiaofei Wang, Chandra Erdman, and John W. Emerson

**See Also**

[legacyplot](#), [bcp](#), [summary.bcp](#), and [print.bcp](#) for complete results and summary statistics.

**Examples**

```
testdata <- cbind( c(rnorm(50), rnorm(50, -5, 1), rnorm(50)),
  c(rnorm(50), rnorm(50, 10.8, 1), rnorm(50, -3, 1)) )
bcp.0 <- bcp(testdata)
plot(bcp.0, main="Multivariate (k=2) Change Point Example")
plot(bcp.0, separated=TRUE, main="Multivariate (k=2) Change Point Example")
```



---

QuebecRivers

*Quebec river streamflow data*

---

## Description

Annual January to June streamflow amounts (measured in  $L/(km^2s)$ ) for four rivers in Quebec: Baleine, Churchill Falls, Manicouagan, and Romaine.

## Usage

QuebecRivers

## Format

A matrix containing streamflow amounts for the years 1972 to 1994.

## Source

The data can be obtained from the Centre d'expertise hydrique Quebec. <https://www.cehq.gouv.qc.ca/hydrometrie/index-en.htm>

## References

1. Xiaofei Wang and John W. Emerson (2015). Bayesian Change Point Analysis of Linear Models on General Graphs, *Working Paper*.
2. L. Perrault *et al.* (2000). Retrospective multivariate Bayesian change-point analysis: a simultaneous single change in the mean of several hydrological sequences, *Stochastic Environmental Research and Risk Assessment*, **14**, 243-261.

## Examples

```
data("QuebecRivers")
bcpr.rivers <- bcp(QuebecRivers)
plot(bcpr.rivers, main="Quebec River Streamflow Change Point Analysis",
      xlab="Year", xaxlab = 1972:1994)
```

---

RealInt	<i>US Ex-post Real Interest Rate data, 1961(1):1986(3)</i>
---------	--

---

**Description**

US ex-post real interest rate: the three-month treasury bill deflated by the CPI inflation rate.

**Usage**

RealInt

**Format**

A quarterly time series from 1961(1) to 1986(3).

**Source**

The data is available online in the data archive of the *Journal of Applied Econometrics*. url: <http://qed.econ.queensu.ca/jae/2003-v18.1/bai-perron/>.

**References**

1. J. Bai and P. Perron (2003), Computation and Analysis of Multiple Structural Change Models, *Journal of Applied Econometrics*, **18**, 1-22. <http://qed.econ.queensu.ca/jae/2003-v18.1/bai-perron/>.
2. Achim Zeileis, Friedrich Leisch, Kurt Hornik, Christian Kleiber (2002), strucchange: An R Package for Testing for Structural Change in Linear Regression Models, *Journal of Statistical Software*, **7**(2), 1-38. <http://www.jstatsoft.org/v07/i02/>.

**Examples**

```
demo(RealInt)
```

---

residuals.bcp	<i>Extract model residuals</i>
---------------	--------------------------------

---

**Description**

residuals method for class bcp.

**Usage**

```
## S3 method for class 'bcp'
residuals(object, ...)
```

**Arguments**

object            the result of a call to bcp().  
 ...              (optional) additional arguments, ignored.

**Value**

Residuals extracted from the bcp object.

**Author(s)**

Xiaofei Wang, Chandra Erdman, and John W. Emerson

**See Also**

[bcp](#) and [plot.bcp](#)

**Examples**

```
##### A random sample from a few normal distributions #####
testdata <- c(rnorm(50), rnorm(50, 5, 1), rnorm(50))
bcp.0 <- bcp(testdata)
residuals(bcp.0)
```

---

summary.bcp

*Summarizing Bayesian change point analysis results*

---

**Description**

Summary and print methods for class bcp.

**Usage**

```
## S3 method for class 'bcp'
summary(object, digits = max(3, .Options$digits - 3), ...)

## S3 method for class 'bcp'
print(x, digits = max(3, .Options$digits - 3), ...)
```

**Arguments**

object            the result of a call to bcp().  
 digits            the number of digits displayed in the summary statistics.  
 ...              (optional) additional arguments, ignored.  
 x                 the result of a call to bcp().

## Details

The functions print (and return invisibly) the estimated posterior probability of a change point for each position and the estimated posterior means. These results are modeled after the summary method of the coda package (Plummer *et al.*, 2006). If `return.mcmc=TRUE` (i.e., if full MCMC results are returned), bcp objects can be converted into mcmc objects to view mcmc summaries – see examples below.

## Value

The matrix of results is returned invisibly.

## Author(s)

Xiaofei Wang, Chandra Erdman, and John W. Emerson

## See Also

[bcp](#) and [plot.bcp](#).

## Examples

```
##### A random sample from a few normal distributions #####
testdata <- c(rnorm(50), rnorm(50, 5, 1), rnorm(50))
bcp.0 <- bcp(testdata)
summary(bcp.0)
plot(bcp.0, main="Univariate Change Point Example")

##### An MCMC summary from the ``coda'' package #####
## Not run:
if (require("coda")) {
  bcp.0 <- bcp(testdata, return.mcmc=TRUE)
  bcp.mcmc <- as.mcmc(t(bcp.0$mcmc.means))
  summary(bcp.mcmc)
  heidel.diag(bcp.mcmc) # an example convergence diagnostic
  # from the coda package.
}

## End(Not run)
```

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